

Robert Brühl, Hartmut Fricke, Michael Schultz  
Institute of Logistics and Aviation  
Chair of Air Transport Technology and Logistics

# Air taxi flight performance modeling and application

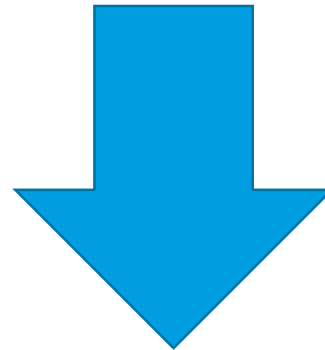
Fourteenth USA/Europe Air Traffic Management Research and Development Seminar (ATM2021)  
20 September 2021

# Agenda

- 1) Problem statement
- 2) Operational background
  - a) UAM flight mission profile
  - b) eVTOL aircraft concepts
- 3) Methodology
  - a) Power & energy requirements
  - b) Model application
- 4) Results
- 5) Conclusion

# Problem statement

- Various aircraft concepts for flying electrical → different behaviour concerning flight performance
- Battery is the central element → most limiting factor in terms of flight range and endurance of electric vertical take-off and landing aircraft (eVTOL)
- No real world range data available since there are only prototypes → range data published by eVTOL manufacturers
- For later network design, the range is one of the most important capabilities of eVTOLs
- **Central problem: manufacturers data vs. real world conditions**



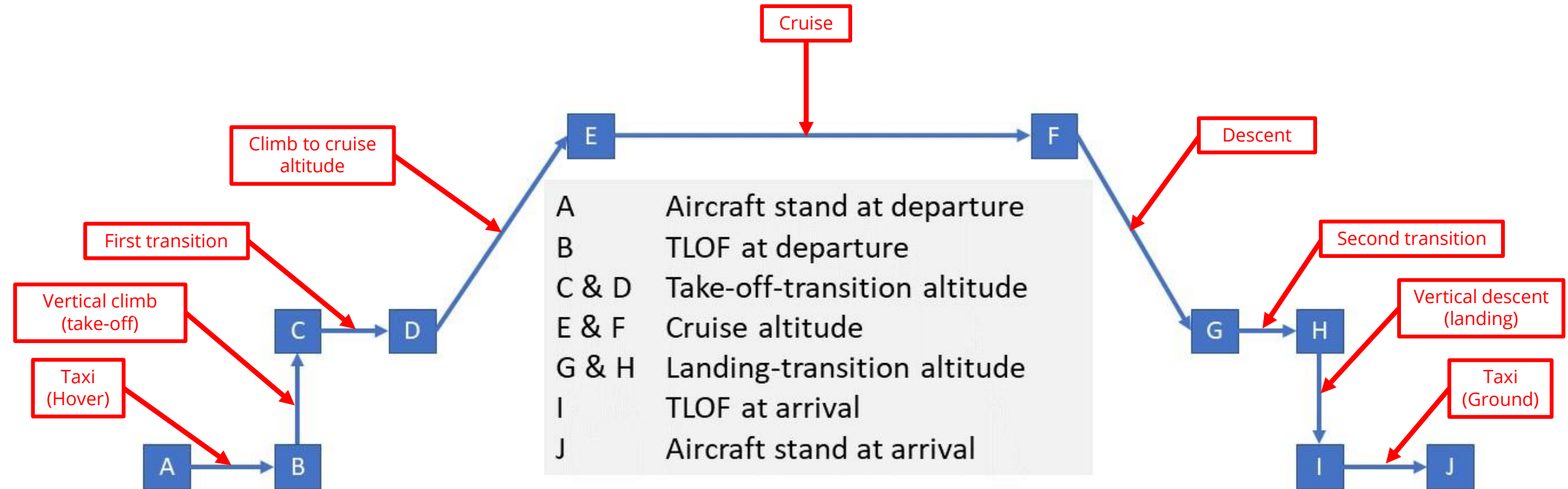
**Does published range data express future reality of air taxi services?**

# Operational background



# Operational background

## a) UAM flight mission profile



# Operational background

## b) eVTOL aircraft concepts

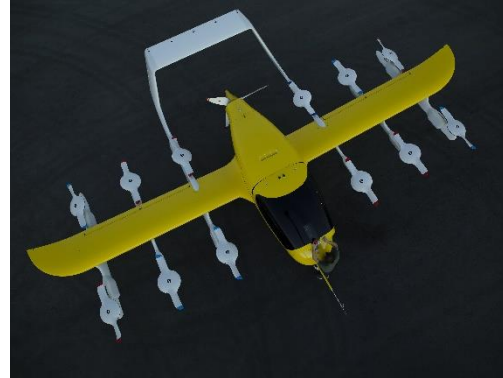
### *Vecored thrust*



Source: <https://newatlas.com/aircraft/joby-aviation-evtol-video/>

- Use of any propulsion unit for vertical and horizontal segments
- Tilting elements to adjust propulsion vector
- Behavior like a fixed-wing aircraft during cruise
- More efficient during cruise; less during vertical segments
- Higher range and speed capabilities

### *Lift & cruise*



Source: <https://twitter.com/WiskAero/status/973711770853535744?s=20>

- Independent propulsion units for vertical and horizontal segments
- No tilting elements
- Behavior like a fixed-wing aircraft during cruise
- More efficient during cruise; less during vertical segments
- Higher range and speed capabilities

### *Multicopter*



Source: <https://www.volocopter.com/solutions/volocity/>

- Multiple horizontally mounted rotors
- Comparable to conventional helicopters (rotary-wing aircraft)
- Higher efficiency during vertical segments
- Limited range and speed capabilities

# Methodology



# Methodology

## a) Power & energy requirements (1)

Power requirements per flight segment:

- (Hover)Taxi: 
$$P_{ht} = \frac{W}{\eta_{hover}} \cdot \sqrt{\frac{DL}{2\rho}} \quad (1)$$

- Vertical climb (take-off): 
$$P_{to} = P_h \cdot \left[ \frac{RoC_{to}}{2v_h} + \sqrt{\left(\frac{RoC_{to}}{2v_h}\right)^2 + 1} \right] \quad (2)$$

- First transition: 
$$P_{trans} = P_{induced} + P_{drag,rotor} + P_{drag,aircraft} \quad (3)$$

$$P_{induced} = \frac{W}{\eta_{trans} \cdot \sin \theta_{tilt}} \cdot \sqrt{-\frac{V_\infty^2}{2} + \sqrt{\left(\frac{V_\infty^2}{2}\right)^2 + \left(\frac{W}{\sin \theta_{tilt} \cdot 2\rho A}\right)^2}} \quad (4)$$

$$P_{drag,rotor} = \rho A V_{tip}^3 \cdot \left(\frac{\sigma C_d}{8} \cdot (1 + 4.6\mu^2)\right) \quad (5)$$

$$P_{drag,aircraft} = 0.5\rho V_\infty^3 C_D S \quad (6)$$

$DL$	Disc loading
$RoC_{to}$	Rate of climb take-off
$v_h$	Velocity hover
$V_\infty$	Induced velocity rotor disc plane
$V_{tip}$	Blade tip velocity
$\sigma$	solidity
$C_d$	Drag coefficient blade
$\theta_{tilt}$	Tilt angle
$C_D$	Drag coefficient aircraft
$S$	Wing surface
$\mu$	Velocity ratio at rotor disc plane
$A$	Total disc area



# Methodology

## a) Power & energy requirements (2)

- Climb to cruise altitude:  $P_{climb} = \frac{W}{\eta_{climb}} \left( RoC_{cl} + \frac{V_{climb}}{\left(\frac{L}{D}\right)_{climb}} \right)$  (7)

- Cruise and descent:  $P_{cruise} = \frac{W \cdot V_{cruise}}{\left(\frac{L}{D}\right)_{cruise} \cdot \eta_{cruise}}$  (8)

- Second transition:  $P_{trans,2} = P_{induced,2} + P_{drag,rotor} + P_{drag,aircraft,2}$  (9)

$$P_{induced,2} = \frac{W}{\eta_{trans} \cdot \sin \theta_{tilt}} \cdot \sqrt{-\frac{V_d^2}{2} + \sqrt{\left(\frac{V_d^2}{2}\right)^2 + \left(\frac{W}{\sin \theta_{tilt} \cdot 2\rho A}\right)^2}} \quad (10)$$

$$P_{drag,rotor} = \rho A V_{tip}^3 \cdot \left(\frac{\sigma C_d}{8} \cdot (1 + 4.6\mu^2)\right) \quad (5)$$

$$P_{drag,aircraft,2} = 0.5\rho V_d^3 C_D S \quad (11)$$

$V_{climb}$	Climb out speed
$RoC_{cl}$	Rate of climb during climb segment
$\frac{L}{D}$	Lift to drag ratio (during climb and cruise)
$V_d$	Horizontal descent speed

# Methodology

## a) Power & energy requirements (3)

- Vertical descent (landing):

$$P_{vd} = P_h \cdot \left[ \frac{RoD_{ld}}{v_h} + \frac{v_i}{v_h} \right] \quad (12)$$

- (Ground)Taxi:

$$P_{gt} = 0.1 \cdot P_{cruise} \quad (13)$$

Energy demand  $E$  per flight segment  $i$ :

- General expressed by product of power  $P_i$  and time  $t_i$ :  $E_i = P_i \cdot t_i$  (14)

- With  $n$  segments the total Energy  $E_{tot}$  becomes:  $E_{tot} = \sum_{i=1}^n E_i = \sum_{i=1}^n P_i \cdot t_i$  (15)

Range estimation:

- range equation for electric flight:

$$R = E^* \cdot \eta_{tot} \cdot \frac{1}{g} \cdot \frac{L}{D} \cdot \frac{m_{battery}}{m_{aircraft}} \quad (16)$$

$v_i$	Induced velocity during vertical segments
$RoC_{ld}$	Rate of climb vertical descent
$E^*$	Specific energy
$m_{battery}$	Battery mass
$m_{aircraft}$	Aircraft mass

# Methodology

## b) Model application – assumptions

### Battery parameters

	Vectored Thrust	Lift & Cruise	Multicopter
$E^* \left[ \frac{Wh}{kg} \right]$	150	180	180
$P^* \left[ \frac{W}{kg} \right]$	2,100	1,600	1,100
$\eta_{tot} [-]$	0.95	0.95	0.95
$DoD [-]$	0.8	0.8	0.8
$m_{battery} [kg]$	730	400	300
$E_{use} [kWh]$	83	55	41
$P_{use} [kW]$	1,165	486	251

### General assumptions

- Consideration of additional power requirements due to losses of the propulsion system by introducing several efficiency values
- Cruise speed chosen according to 80% of maximum speed published by manufacturers
- Calculation and results based on the maximum take-off mass (MTOM) of each eVTOL
- Range estimation based on specific energy for cruise and descent segment ( $E^*_{cruise}$ )

### Flight mission time

Segment	Time [s]
First taxi	30
Take-off	45
First transition	45
Climb	60
Cruise & descent	1,500
Second transition	45
Landing	45
Second taxi	30
<b><math>\Sigma</math></b>	<b>1,800</b>

# Results



# Results

## Power Requirements

- Transition segments = peak power demanding segments for vectored thrust and lift & cruise eVTOL, whereas it is the climb for multicopter
- The power demand during transition of vectored thrust eVTOL exceeds  $P_{use}$  by 22.8% and 41.7% for lift & cruise
- Power demand for all other segments is lower than  $P_{use}$
- Power demand for multicopter in all segments is lower than  $P_{use}$

## Energy demand

- Excess of energy demand compared to  $E_{use}$ :
  - vectored thrust by 37% and
  - multicopter by 11%
- Lift & cruise eVTOL has reserve of 11% after assumed mission
- Multicopter would be able to perform flight mission when using total energy (16% reserve in that case)

## Range estimation

- Estimation is only based on the time of cruise and descent segment (corresponding  $E_{cruise}^*$ )
- Only theoretical, because eVTOL would not be able to perform the assumed mission according to results of power and energy requirements
- Vectored thrust: 115 km (vs. 240 km)
- Lift & Cruise: 70 km (vs. 40 km)
- Multicopter: 50 km (vs. 35 km)

# Conclusion



# Conclusion

- Expectation that vertical segments / transition = peak power / energy demanding segments is proven (the chosen values for specific power and energy are not sufficient)
- Simplification of using  $\rho$  at MSL:
  - Influences of altitude and temperature are neglected within our framework
- Battery parameters = central factor
  - Value of specific power affects and limits performing capability of vertical segments
  - Value of specific energy influences achievable range
- To increase range → maximizing of:
  - Battery mass ratio (increasing battery mass by a constant aircraft mass)
  - Lift over drag ratio
  - Total system efficiency
  - Energy density → values of 450 Wh/kg expected in future → possible ranges:
    - Vectored thrust: 260 km
    - Lift & cruise: 190 km
    - Multicopter: 120 km

# Thank you for your attention!

robert.bruehl@tu-dresden.de

