

# Combining Flight Level Allocation with Ground Holding to Optimize 4D-Deconfliction

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# Introduction

## Congested European Sky

- Regulation delays mainly due to en-route sector capacities
- Structural limits of the sector-based ATC system reached
- Optimization of airspace structure and ATFM regulations: SESAR

## Two-Stage ATM Optimization

- 1 Flight Level Allocation
  - Vertical separation of 2D + time-intersecting flights
  - Graph Coloring, but minimization of discrepancy to requested FL
- 2 Ground Holding
  - Deconfliction by departure time adjustment
  - Graph Coloring as special case, minimization of delays

## Solved by Constraint Programming (CP)

- Versatile modelling tool for combinatorial optimization problem
- Optimality proof for feasibility stage

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## Pre-tactical Flow Regulation

- **Safer** than handling the traffic while airborne
- **Costly** for airspace users, network effect

## Sector Capacity and Regulation

- Air Traffic Control Centres **opening schedules**: designed by experts, based on previous traffic and demand
- Open sectors **capacities**: hourly entry rate
- **Regulation** on flows crossing overloaded sectors: Computer Assisted **Slot Allocation** (CASA/ETFMS) at CFMU

## Accuracy and Effectiveness of the Model?

- **Relevance** of sector capacity to model **controller workload**?
- **Discrepancies** between planned schedule and actual openings
- CASA: **greedy** algorithm (optimality soundness?)

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# 4D-Trajectory Deconfliction

## 4D-Trajectory Planning

- “Strategic” deconfliction (EC project Episode 3)
- Several opportunities: flight level, rerouting, delay, speed...
- Large scale combinatorial optimization problems

## Conflict Model

- **Finest** grain (conflicts) vs aggregated model (sector capacity)
- **Sliding time windows** to handle **uncertainty**

## Two-Stage Trajectory Deconfliction

### 1 Flight Level Allocation

- Detection in the horizontal plane
- Vertical separation (Graph Coloring) **minimizing discrepancy to RFL**

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- **Minimization of delays**

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## Data

- **Flight plans** and airspace data for one day of traffic
- **Simulation** with CATS [Alliot, Durand 97]
- **Trajectories sampled** every 15s (catch shortest conflicts)
- Notation: flight  $i$  at point  $p_i^k$  at time  $t_i^k$  if not delayed

## Variables and Constraints

- **Decision variables:** flight level  $FL_i \in [RFL_i - \text{dev}_{\max}, RFL_i + \text{dev}_{\max}]$  and delay  $\delta_i \in [0, \delta_{\max}]$  for each flight  $i$
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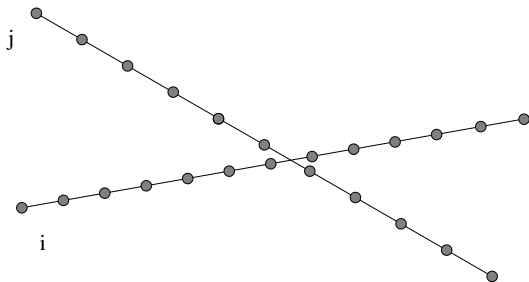
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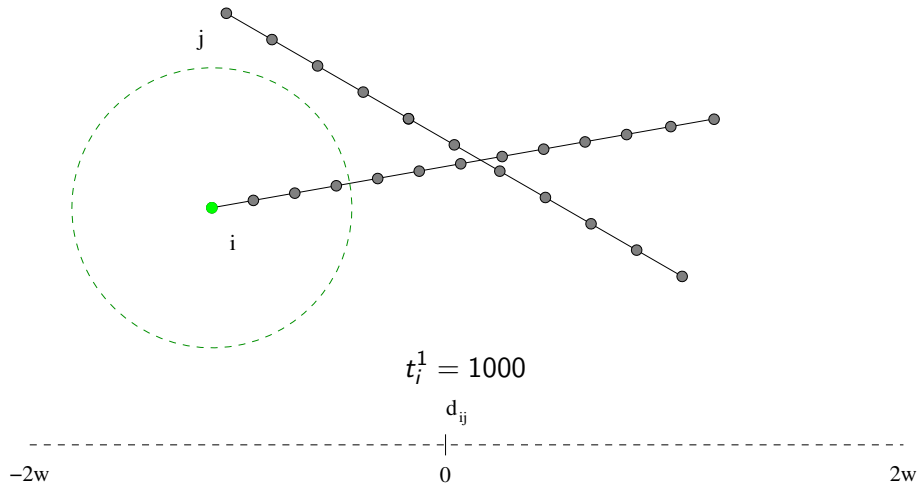
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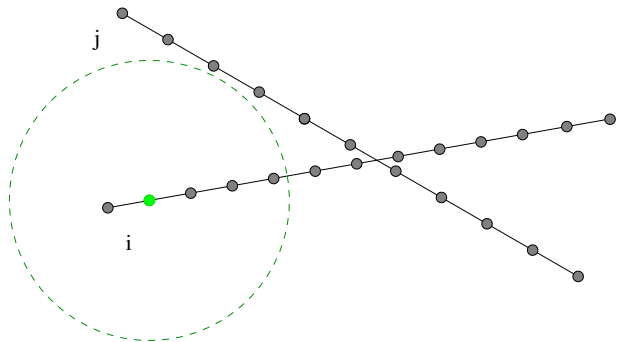
$$t_i^k \in [1000, 1180], t_j^l \in [600, 750]$$

 $d_{ij}$ 
 $-2w$ 
 $0$ 
 $2w$

# Conflict Detection



# Conflict Detection



$$t_i^2 = 1015$$

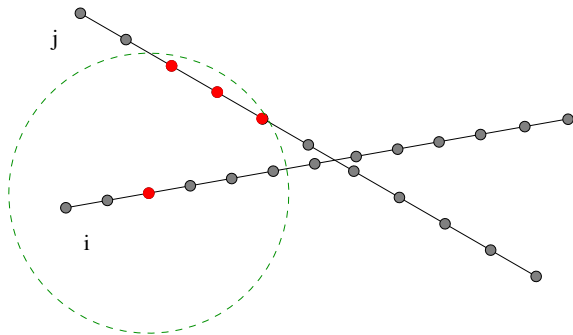
$$d_{ij}$$
 $-2w$ 

0

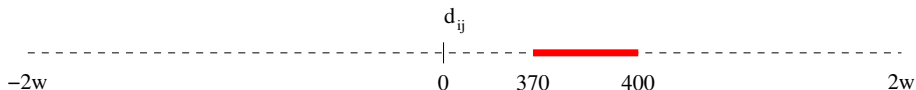
 $2w$



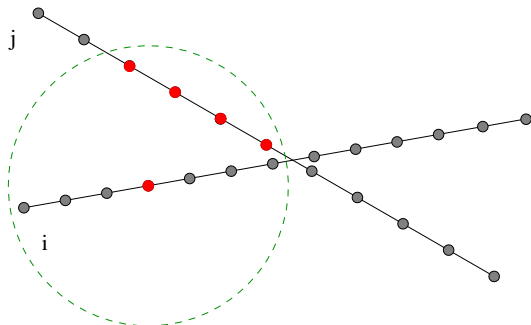
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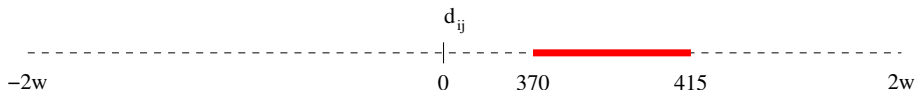
$$t_i^3 = 1030, [t_j^3 = 630, t_j^5 = 660], d_{ij} \notin [370, 400]$$



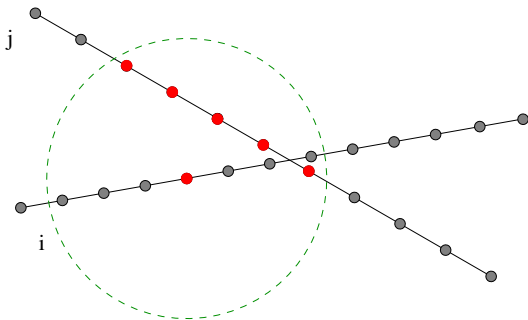
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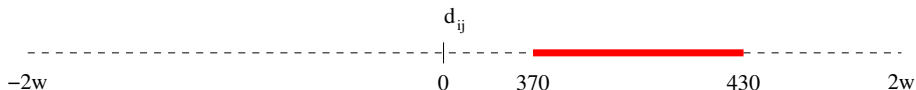
$$t_i^4 = 1045, [t_j^3 = 630 - t_j^6 = 675], d_{ij} \notin [370, 415] \subseteq [370, 415]$$



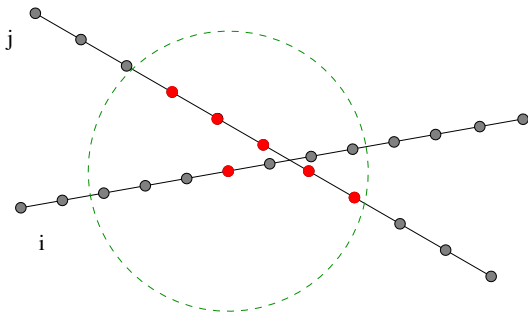
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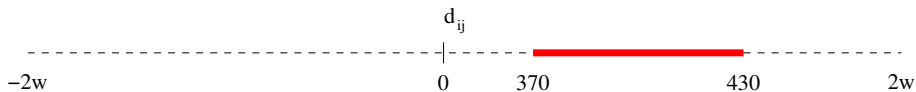
$$t_i^5 = 1060, [t_j^3 = 630 - t_j^7 = 690], d_{ij} \notin [370, 430] \subseteq [370, 430]$$



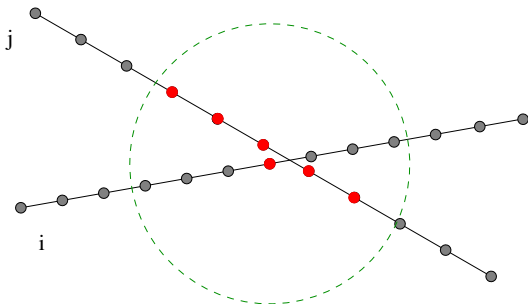
# Conflict Detection



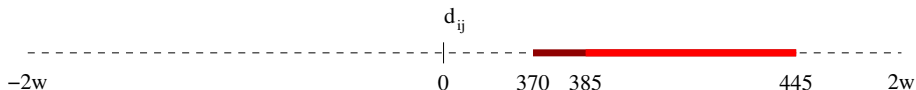
$$t_i^6 = 1075, [t_j^4 = 645 - t_j^8 = 705], d_{ij} \notin [370, 430] \subseteq [370, 430]$$



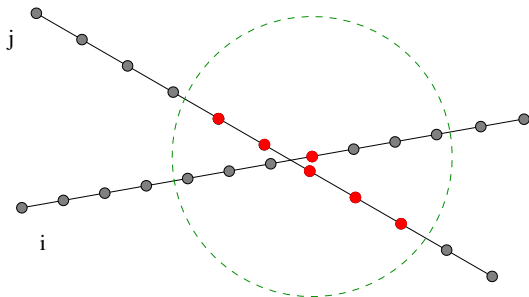
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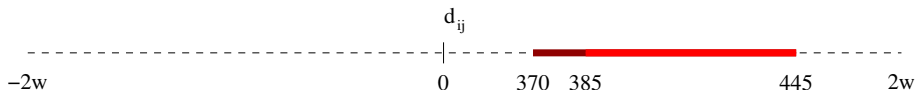
$$t_i^7 = 1090, [t_j^4 = 645 - t_j^8 = 705], d_{ij} \notin [385, 445] \subseteq [370, 445]$$



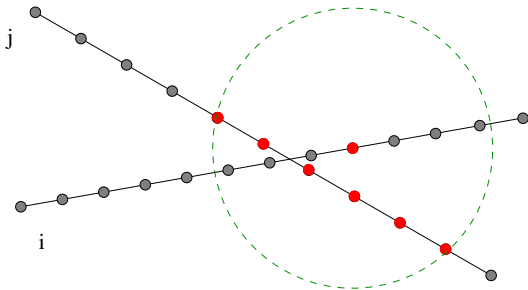
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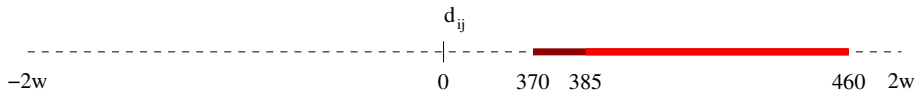
$$t_i^8 = 1105, [t_j^5 = 660 - t_j^9 = 720], d_{ij} \notin [385, 445] \subseteq [370, 445]$$



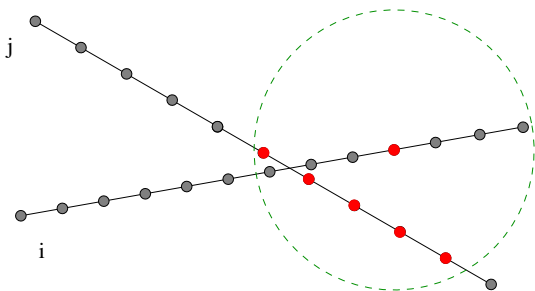
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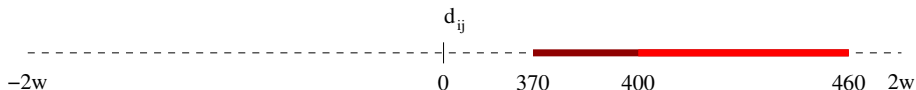
$$t_i^9 = 1120, [t_j^5 = 660 - t_j^{10} = 735], d_{ij} \notin [385, 460] \subseteq [370, 460]$$



# Conflict Detection

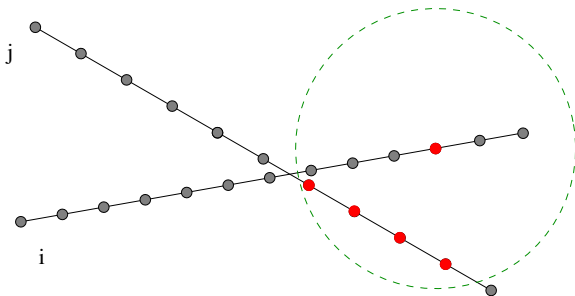


$$t_i^{10} = 1135, [t_j^6 = 675 - t_j^{10} = 735], d_{ij} \notin [400, 460] \subseteq [370, 460]$$

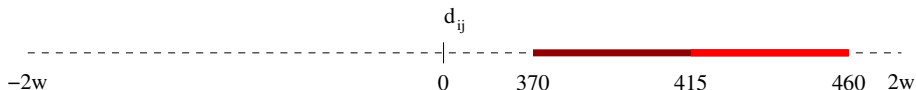




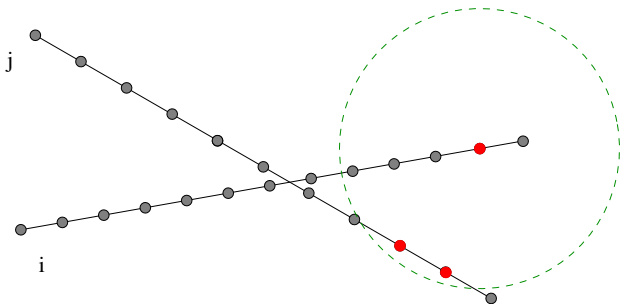
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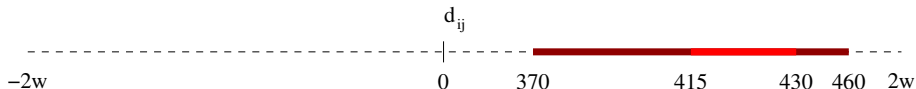
$$t_{11}^i = 1150, [t_j^7 = 690 - t_j^{10} = 735], d_{ij} \notin [415, 460] \subseteq [370, 460]$$



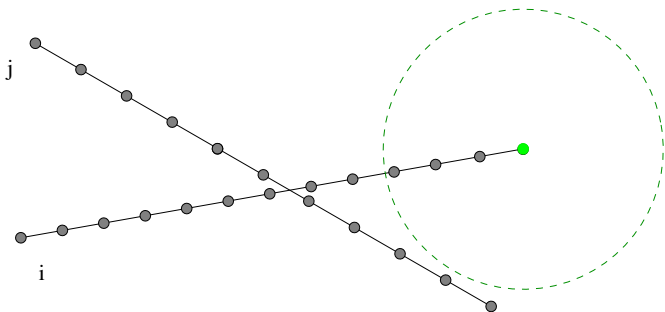
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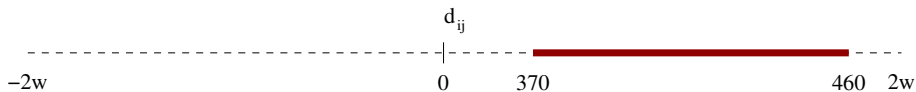
$$t_{12}^i = 1165, [t_j^9 = 720 - t_j^{10} = 735], d_{ij} \notin [415, 430] \subseteq [370, 460]$$



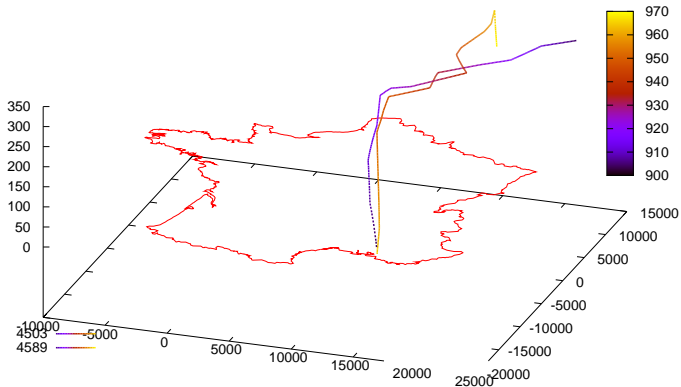
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$$d_{ij} = \delta_j - \delta_i \notin [370, 460]$$



# Multiply-Conflicting Flight Pair

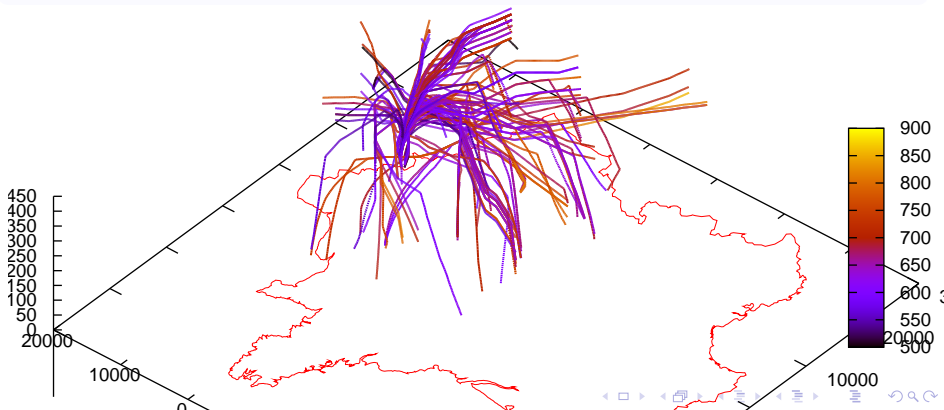


$$d_{ij} = \delta_j - \delta_i \notin C_{ij} = [lb_{ij}^1..ub_{ij}^1] \cup \dots \cup [lb_{ij}^k..ub_{ij}^k]$$

# Flight Conflicting with Many Other

## Constraint Graph of High Degree

- Highest degree  $> 650$
- Large cliques  $> 150$
- One single large connected component



## 2D+Time Conflicts

For each pair of flights  $i \neq j$

$\forall k, l$ , such that  $d_h(p_i^k, p_j^l) < 5 \text{ NM}$  (horizontal plane only):

$$\theta_i^k \neq \theta_j^l$$

$$t_i^k + \delta_i \neq t_j^l + \delta_j$$

$$d_{ij} \neq t_i^k - t_j^l$$

Therefore:  $d_{ij} \notin C_{ij}^H = [lb_{ij}^1..ub_{ij}^1] \cup \dots \cup [lb_{ij}^m..ub_{ij}^m]$

We note:  $conflict^H(i, j) \Leftrightarrow [-\delta_{\max}, \delta_{\max}] \cap C_{ij}^H \neq \emptyset$

Trajectories truncated to their largest possible level part  
(below  $RFL - dev_{\max}$ )

# FL Allocation: Flows Model

## Model

- Flights sharing the same route and (almost) same RFL aggregated into flows  $\mathcal{F}_k$
- Extension of conflicts to flows:

$$\text{conflict}(\mathcal{F}_k, \mathcal{F}_l) \Leftrightarrow \exists (i, j) \in \mathcal{F}_k \times \mathcal{F}_l \text{ s.t. } \text{conflict}^H(i, j)$$

$$\text{Constraints:} \quad \text{conflict}(\mathcal{F}_k, \mathcal{F}_l) \Rightarrow FL_k \neq FL_l$$

$$\text{Cost:} \quad \text{cost}_{FL} = \sum_i |RFL_i - FL_i|$$

## Limits

- Few variables, but very dense constraint graph
- Does not solve catch-up conflicts

It was abandoned for the single flight model.

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For each pair of flights  $i \neq j$

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## Temporal Relaxation

- Very dense graph with costly solutions for feasible values of  $\delta_{\max}$
- Most flights won't be delayed (or by a very small amount)
- Detection with  $d_{ij} = 0 \in \mathcal{C}_{ij}^H$ : solutions with low  $\text{dev}_{\max}$  and  $\text{cost}_{FL}$

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# Ground Holding Conflict Constraints

For each pair of flights  $i \neq j$  after FL allocation

$\forall k, l$ , such that  $d_h(p_i^k, p_j^l) < 5 \text{ NM} \wedge d_v(p_i^k, p_j^l) < 1000 \text{ ft}$ :

$$\theta_i^k \neq \theta_j^l$$

Therefore:

$$d_{ij} \notin C_{ij} = [lb_{ij}^1 .. ub_{ij}^1] \cup \dots \cup [lb_{ij}^m .. ub_{ij}^m]$$

Cost:

$$\text{cost}_{GH}^{\max} = \max_i \delta_i$$

$$\text{cost}_{GH}^{\text{sum}} = \sum_i \delta_i$$

*NP-hard problem*

## Non European Flights

- Flights originating outside the ECAC zone cannot be delayed by Eurocontrol instances ( $\approx 10\%$ ):  $\delta_i = 0$
- Conflicts between two such flights discarded (a few dozens)

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# Results

## Instance Figures

- Traffic within French airspace in 2008 (time step: 1 min)
- Demand up to 8 700 flights
- Up to 37 000 intersecting flights during FL allocation
- Up to 315 000 during ground holding

## Resolution

- All instances solved down to FL0 (except TMA)
- **Max optimality proof** for most of them
- A few seconds for FL allocation and about 1 min for ground holding
- No optimization of the mean/sum but minimizing search heuristic

# Results

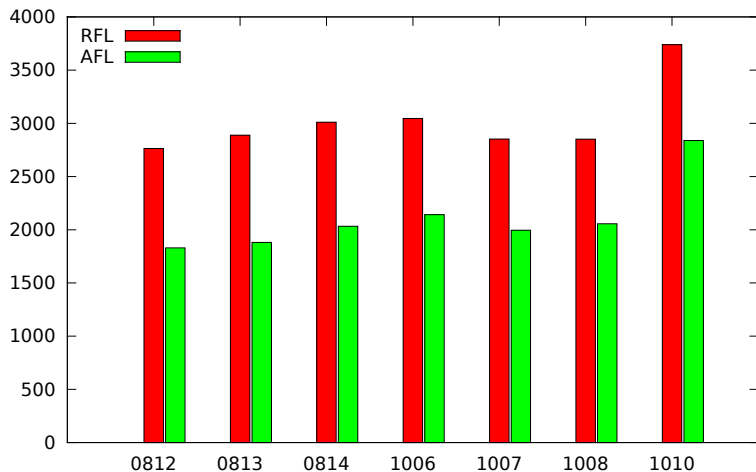
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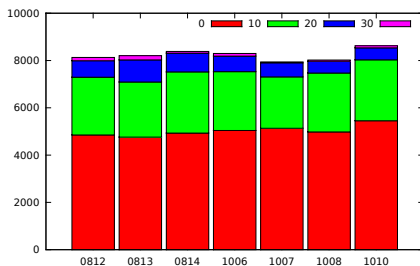
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# Reduction of the Number of Conflicts After FL Allocation

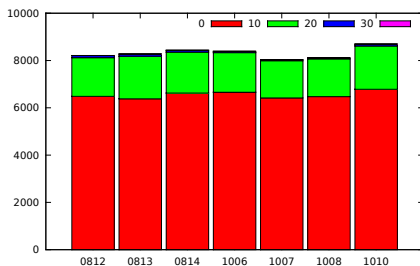


- Cannot take climb/descent phase into account ( $\approx 75\%$  of all conflicts)
- All cruising phase conflicts solved for  $dev_{\max} = FL30$

# Distribution of Discrepancies from RFL After Allocation



Flows Model

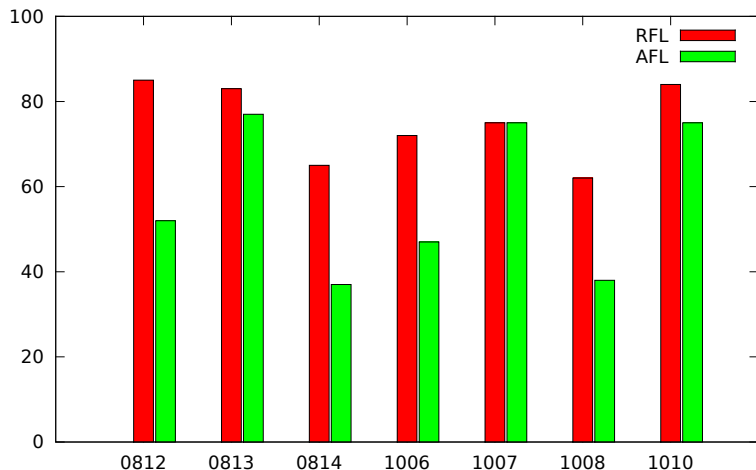


Single Flight Model

- Cost with Single Flight Model 55% better than with Flows Model
- All instances solved with  $dev_{\max} = FL30$ ,  $cost_{FL} = 16\,000 - 20\,000$
- 80% at their RFL, 20% at FL10, 1% at FL20 and a couple at FL30

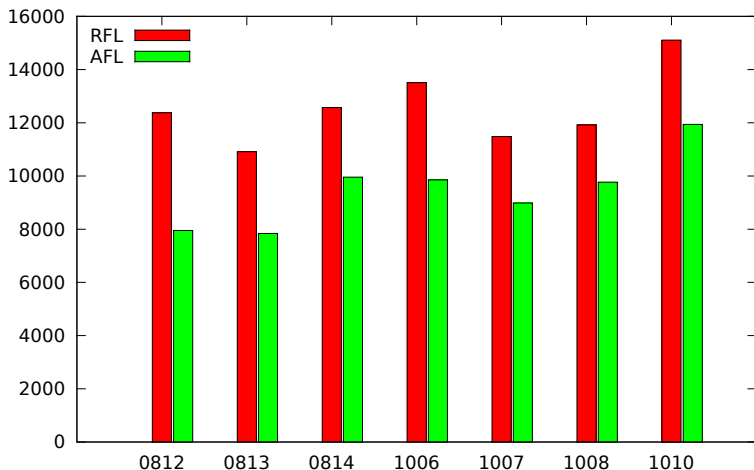


# Optimal Max Cost Before and After FL Allocation



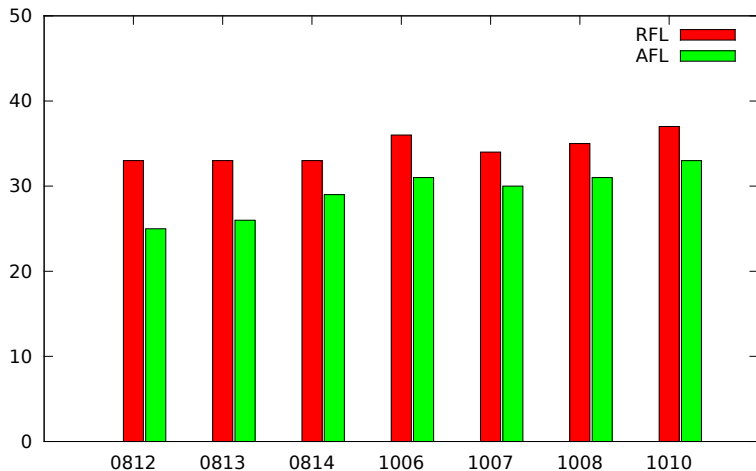
- Reduction up to 40% (average 25%)
- But max criterion does not reflect the overall amount of delay

# Sum of delays before and after FL allocation



- Reduced by 25% on average (up to 36%)
- More consistent than max delay

# Percentage of delayed flights before and after FL allocation



- Reduced by 5% on average (up to 8%)

# Further Works

## More Realistic Modelling

- **Temporal uncertainties** taken into account in real time with iterative resolution over a **sliding time window**
- Side constraints: aircraft rotation (easy to implement but lack of data)...
- Handling remaining conflicts with CATS resolution modules [Granger, Durand, Alliot 2001] (horizontal manoeuvres, speed adjustment)

## European Instances

- Up to 30 000 flights a day
- More RAM or other search paradigms (LS, meta-heuristics, combination with CP)

# Further Works

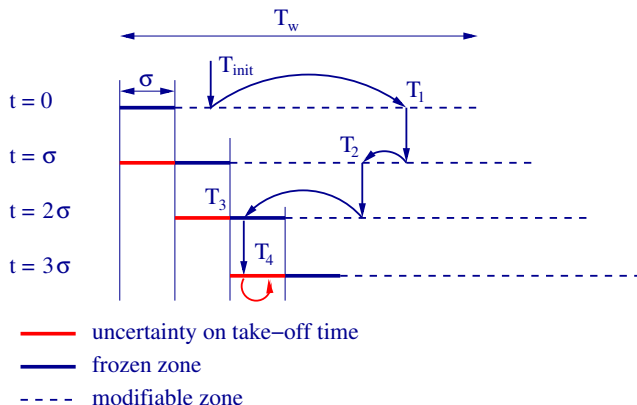
## More Realistic Modelling

- **Temporal uncertainties** taken into account in real time with iterative resolution over a **sliding time window**
- Side constraints: aircraft rotation (easy to implement but lack of data)...
- Handling remaining conflicts with CATS resolution modules [Granger, Durand, Alliot 2001] (horizontal manoeuvres, speed adjustment)

## European Instances

- Up to 30 000 flights a day
- More RAM or other search paradigms (LS, meta-heuristics, combination with CP)

# Handling Uncertainties with Sliding Time Window



- Flights with departure time between  $t - \sigma$  and  $t$  are “noised”
- If the uncertainty brings them back to the “modifiable zone”, they are taken into account again for allocation

# Conclusion

## ATM

- **Flight level allocation** and **ground holding** combined
- **Deconfliction** vs aggregated regulation
- FL allocation with very low discrepancies to RFL
- Amount of allocated **delay compatible with typical CFMU figures**
- Large problem but **optimality proof** (w.r.t. max) obtained with CP
- Has to be **combined with other strategies** (e.g. sliding windows) when managing uncertainties

## CP

- **Versatile** technology: quick prototyping, various search strategies, incremental refinement of the model, side constraints...
- CP technology **scalable** to such LSCOP, even with ECAC instances?
- May be **combined** with other search paradigms: LS to solve CSP, CP to speed up LS...



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